

EXAMPLE: 6/124

G5

50 kg FLYWHEEL; radius of gyration = 0.4 m about shaft

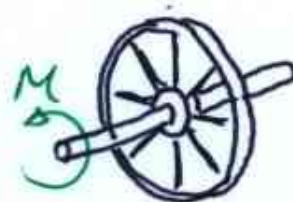
TORQUE APPLIED: $M = 2(1 - e^{-0.1\theta})$ N.m θ in radians

@ $\theta = 0$, flywheel @ rest
after 5 revs what's ω ?

Energy Equation:

$$T_2 = T_1 + U_{1 \rightarrow 2}$$

↓ FINAL kin. Energy kinetic energy @ start NO POTENTIAL ENERGY WORK DONE



$T_1 = 0$ because $\omega = 0$ @ $\theta = 0$

find $U_{1 \rightarrow 2}$

$$\begin{aligned} U_{1 \rightarrow 2} &= \int_0^{10\pi} M d\theta = \int_0^{10\pi} 2(1 - e^{-0.1\theta}) d\theta \\ &= [2\theta + 20e^{-0.1\theta}]_0^{10\pi} \\ &= (2 \times 10\pi + 20e^{-0.1(10\pi)}) - (20) \end{aligned}$$

$$U_{1 \rightarrow 2} = \underline{43.7} \text{ J} = T_2$$

$$I_G = mk_G^2$$

$$T_2 = \frac{1}{2} \underset{m}{I_G} \omega^2 = \frac{1}{2} (50) \underset{k_g^2}{(0.4)^2} \omega^2 = 4\omega^2$$

$$\therefore 43.7 = 4\omega^2 \Rightarrow \boxed{\omega = 3.31 \text{ rad/s}}$$